

The total distance travelled by the light pulse in the reference frame of a stationary observer is twice the length of one diagonal (d) (Figure 1.58) which is calculated using Pythagoras' theorem.

$$d = 2 \times \sqrt{L^2 + \left(\frac{vt}{2}\right)^2}$$

The time interval (t) between events A and B inside the spacecraft as measured in the reference frame of a stationary observer is determined using the formula derived below*.

$t = \frac{d}{c}$	$t = 4L^2 + v^2t^2$
$t = \frac{2 \times \sqrt{L^2 + \left(\frac{vt}{2}\right)^2}}{c}$	$4L^2 = c^2 \times t^2 - v^2t^2$
$ct = 2 \times \sqrt{L^2 + \left(\frac{vt}{2}\right)^2}$	$4L^2 = (c^2 - v^2) t^2$
$c^2t^2 = 2^2 \times L^2 + \left(\frac{vt}{2}\right)^2$	$\frac{4L^2}{c^2} = \left(\frac{c^2 - v^2}{c^2}\right) t^2$
$c^2t^2 = 4L^2 + \left(\frac{v^2t^2}{4}\right)$	$\frac{4L^2}{c^2} = \left(\frac{c^2 - v^2}{c^2} - \frac{v^2}{c^2}\right) t^2$
$c^2t^2 = \frac{4L^2}{1} + \left(\frac{v^2t^2}{4}\right)$	$\frac{4L^2}{c^2} = \left(1 - \frac{v^2}{c^2}\right) t^2$
$c^2t^2 = \frac{16L^2}{4} + \left(\frac{v^2t^2}{4}\right)$	$\frac{2L}{c} = \sqrt{\left(1 - \frac{v^2}{c^2}\right)} t$
$c^2t^2 = \frac{16L^2 + v^2t^2}{4}$	$t_0 = \sqrt{\left(1 - \frac{v^2}{c^2}\right)} t$
	$t = \frac{1}{\sqrt{\left(1 - \frac{v^2}{c^2}\right)}} t_0$

The light clock example shows that the time interval between events A and B is different in two reference frames that are moving relative to each other. This phenomenon is called **time dilation**.

The time interval (t) between events A and B measured in the reference frame of an observer on Earth is calculated using the formulae below.

Formulae	$t = \frac{1}{\sqrt{\left(1 - \frac{v^2}{c^2}\right)}} t_0$ and $t = \gamma t_0$
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Symbol	Variable	SI unit
t	Time interval in the stationary observer's reference frame	s
t_0	Time interval in the moving reference frame	s
v	Relative velocity between the two reference frames.	m s^{-1}
c	Speed of light in a vacuum	m s^{-1}
γ	The Lorentz factor, $\frac{1}{\sqrt{\left(1 - \frac{v^2}{c^2}\right)}}$	

*This derivation is not assessed and has been included only for interest.